

Papers published in *Hydrology and Earth System Sciences Discussions* are under open-access review for the journal *Hydrology and Earth System Sciences*

Towards model evaluation and identification using Self-Organizing Maps

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Received: 17 October 2007 – Accepted: 19 October 2007 – Published: 5 November 2007

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HESSD

4, 3953–3978, 2007

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Abstract

The reduction of information contained in model time series through the use of aggregating statistical measures is very high compared to the amount of information that one would like to draw from it for model identification and calibration purposes. Applied within a model identification context, aggregating statistical performance measures are inadequate to capture details on time series characteristics. It has been readily shown that this loss of information on the residuals imposes important limitations on model identification and -diagnostics and thus constitutes an element of the overall model uncertainty. In this contribution we present an approach using a Self-Organizing Map (SOM) to circumvent the identifiability problem induced by the low discriminatory power of aggregating performance measures. Instead, a Self-Organizing Map is used to differentiate the spectrum of model realizations, obtained from Monte-Carlo simulations with a distributed conceptual watershed model, based on the recognition of different patterns in time series. Further, the SOM is used instead of a classical optimization algorithm to identify the model realizations among the Monte-Carlo simulations that most closely approximate the pattern of the measured discharge time series. The results are analyzed and compared with the manually calibrated model as well as with the results of the Shuffled Complex Evolution algorithm (SCE-UA).

1 Introduction

Information from existing or additional observed sources is crucial to decrease model uncertainty. Model evaluation and model identification usually resort to aggregating statistical measures to compare observed and simulated time series (Legates and McCabe Jr., 1999). In this context however these measures involve considerable problems (Yapo et al., 1998; Lane, 2007). To certain extent, the choice of performance measures can be made such that the evaluation makes certain emphasis on different parts of the hydrograph (Gupta et al., 1998). Yet aggregating measures of performance

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have in common that the information contained in the errors is aggregated into a single numerical value, regardless of the characteristic and the actual pattern of the error. In consequence, essentially different model results can be obtained with close to identical performance measure values although the parameter sets used to generate them are widely scattered throughout the parameter space. Therefore the information conveyed by aggregating goodness-of-fit measures is likely to be insufficient to unambiguously differentiate between a number of alternative model realizations (and thus cannot give evidence of their equivalence, i.e. equifinality) (Gupta et al., 2003; Beven and Binley, 1992). This lack of discriminatory power imposes important limitations on model identification and constitutes an important source of model uncertainty (Wagener et al., 2003). In contrast, one strong point of the manual calibration procedure resides on the ability to use various complementary information sources, e.g. river discharge, groundwater level or soil moisture observations (Franks et al., 1998; Lamb et al., 1998; Seibert, 2000; Ambroise et al., 1995). In the first instance, however, its success is due to the simultaneous evaluation of numerous different characteristics related to a time series (Gupta et al., 2003) which allows for a much better extraction of information from the available data. Multiple-criteria approaches that seek to emulate this strategy to some extent have therefore considerably improved model identifiability. Important examples of successful applications of this strategy can be found e.g. in Gupta et al. (1998), Boyle et al. (2000), Vrugt et al. (2003) and Wagener et al. (2004). Yet model identification methods that depend on common statistical approaches might still not be able to extract enough information relevant to this task (Gupta et al., 2003). An exciting new point of view for model evaluation and identification that tackles these shortcomings emerges from the transformation of the existing data into the frequency domain and the wavelet domain (e.g. Clemen, 1999; Lane, 2007.).

In order to improve model identifiability (as proposed by Gupta et al., 1998; Yapo et al., 1998 and Boyle et al., 2000) and the extraction of information from existing data we introduce an approach that, in a sense, emulates the visual assessment of model hydrographs. To circumvent the ambiguity induced by standard objective functions

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a Self-Organizing Map (SOM) (Kohonen, 2001) is used to represent the spectrum of model realizations obtained from Monte-Carlo simulations with a distributed conceptual watershed model based on the recognition of different patterns of model residual time series.

Self-Organizing maps have found successful practical applications in speech recognition, image analysis, categorization of electric brain signals (Kohonen, 2001) as well as process monitoring (Alhoniemi et al., 1999; Simula et al., 1999) and local time series modelling (Vesanto, 1997; Principe et al., 1998; Cho, 2004). Similarly diverse are the currently emerging applications of SOM in the field of hydrology: Examples for the analysis of hydrochemical data can be found in Peeters et al. (2007) and Lischeid (2006). Schütze et al. (2005) apply a variant of the SOM to approximate the Richards equation and its inverse solution. Hsu et al. (2002) successfully performed system identification and daily streamflow predictions with the Self-Organizing Linear Output Mapping Network (SOLO). They used a SOM to control local regression functions according to the stage of the rainfall-runoff process. Kalteh and Berndtsson (2007) use SOM for the interpolation of monthly precipitation.

In Sect. 2.1 of this contribution we summarize the principles and advantages of SOM and describe how this method is used to yield a topologically ordered mapping of model output time series according to the similarity in the temporal patterns of their residuals obtained through Monte-Carlo simulations. The properties of this “semantic map” of model realizations will be examined by relating the map elements i) to the standard performance measures of the associated model runs and ii) to the parameter values that have been used to generate the model results. It is shown that a SOM is capable of giving visual insights into the parameter sensitivity and the operating of the model structure. Moreover, in the second part of this article these properties are used to introduce an application of the Self-Organizing Map for parameter identification purposes. The SOM is used instead of a classical optimization algorithm to identify the model realizations from among the Monte-Carlo simulations that most closely approximate the pattern of the measured time series, i.e. the “zero-residual” realization. The result

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will be analyzed and compared with the manually calibrated model as well as with the result of the single-objective Shuffled Complex Evolution algorithm (SCE-UA, Duan et al., 1993).

2 Methods

2.1 The Self-Organizing Map

The Self-Organizing Map is a clustering, visualization and abstraction algorithm that is based on the artificial neural network paradigm and unsupervised learning. Unlike other types of ANN it has no output function. Instead it maps vectorial input data items with similar patterns onto contiguous locations of a discrete low-dimensional grid of neurons in a topology-preserving manner. Therefore its output can be compared to a semantic map. Each of its neurons becomes sensitized to a different domain of the patterns contained in the vectorial training data items, i.e. the map units act as decoder for different types of patterns contained in the input data (Kohonen, 2001).

Each input data item $\mathbf{x} \in X$ is considered as a vector

$$\mathbf{x} = [x_1, x_2, \dots, x_n]^T \in \mathbb{R}^n \tag{1}$$

with n being the dimension of the input data space. A fixed number of k neurons indexed i is arranged on a regular grid G with each neuron being associated to a weight vector

$$\mathbf{m}_i = [\mu_{i1}, \mu_{i2}, \dots, \mu_{in}]^T \in \mathbb{R}^n \tag{2}$$

also called reference vector, which has the same dimensionality as the input vectors $\mathbf{x} \in X$. These weights connect each input vector \mathbf{x} in parallel to all neurons of G . Moreover the neurons are connected to each other. In our case this interconnection is defined on a hexagonal grid topology. The training of the SOM now comprises the following steps:

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1. The components of the \mathbf{m}_i are initialized with a sequence of values from points on the plane spanned by the two greatest eigenvectors of the data distribution. This procedure assures a faster and more reliable convergence of the algorithm (Kohonen, 2001).

5 2. Randomly pick an input vector sample $\mathbf{x} \in X$ and compute the Euclidean distance

$$\|\mathbf{x} - \mathbf{m}_i\| = \sqrt{\sum_{j=1}^n (x_j - m_{ij})^2} \quad (3)$$

between \mathbf{x} and each of the reference vectors \mathbf{m}_i (as a measure of similarity, generally any other metric can be applied as well) and find the neuron $c(\mathbf{x})$ with a reference vector \mathbf{m}_c such that

$$10 \quad \|\mathbf{x} - \mathbf{m}_c\| = \min_i \{\|\mathbf{x} - \mathbf{m}_i\|\} \quad (4)$$

c is then called the best-matching unit (BMU) and defines the image of the sample \mathbf{x} on the map G .

3. The nodes that are within a certain distance of the “winning neuron” c are updated according to the equation

$$15 \quad \mathbf{m}_i(t+1) = \mathbf{m}_i(t) + \alpha(t) h_{ci}(t) [\mathbf{x}(t) - \mathbf{m}_i(t)] \quad (5)$$

where t is the number of the iteration step and $\mathbf{m}_i(t)$ is the current weight vector which is updated proportionally to the difference $[\mathbf{x}(t) - \mathbf{m}_i(t)]$. $h_{ci}(t)$ determines the degree of neighbourhood between the winning neuron c and a neuron i for an input $\mathbf{x} \in X$, i.e. the rate of adaptation in the neighbourhood around c . This function is required to be symmetric about c and decreasing to zero with growing lateral distance from c (Haykin, 1999). Commonly the Gaussian function

$$20 \quad h_{ci}(t) = \exp\left(-\frac{\|r_c - r_i\|^2}{2\sigma^2(t)}\right) \quad (6)$$

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is used, whereas $\|r_c - r_i\|^2$ denotes the lateral distance between the winning neuron and the neuron i .

$\sigma(t)$ defines the width of the topological neighbourhood, which is also monotonically decreasing with t . It is required that $h_{ci}(t) \rightarrow 0$ for $t \rightarrow \infty$. In Eq. (5) $\alpha(t)$ is called the learning rate factor ($0 < \alpha(t) < 1$) which proportionally to the iteration step t monotonically decreases the rate of change of the weight vectors. According to Kohonen (2001) an exact choice of the function is not relevant. With Eq. (5) the training acquires adaptive and cooperative properties through which the weights m_i are updated to move closer towards the winning neuron, similar to an elastic net (Kohonen, 2001).

4. Repeat steps 2 and 3 with the next data vector x until a fixed number of iterations is reached.

Upon repeated cycling through the training data the mapping from the continuous input space X onto the spatially discrete output space G acquires the following properties (Haykin, 1999):

- The reference vectors m_i “follow” the distribution of the input data vectors such that the map G provides a discrete approximation to the input space X . This is as well the reason why dimensionality reduction and data compression properties can be attributed to the SOM. The fix number of weight vectors m_i can be interpreted as pointers for their corresponding neuron into the input space X , hence the elements of m_i can be interpreted as coordinates of the image of this neuron in the input space.
- From Eq. (5) immediately follows the topological ordering property of the mapping computed by the SOM such that the location of a neuron on the grid G represents a particular domain of pattern in the input data. Moreover, this ordering property at the same time provides fault and noise tolerant abilities of the mapping (see also Allinson and Yin, 1999). The local interactions between the neurons provide for the smoothness of the map.
- Patterns in the input space X that occur more frequently are mapped onto a larger

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area in the output space G .

- A SOM has the ability to select a best set of features for approximating an underlying nonlinear distribution corrupted by additive noise. Hence SOM provides a discrete approximation of principle curves, i.e. a generalization of principal component analysis.

In the second part of this contribution we make use of the fact that the SOM can also be applied to project an input data vector \mathbf{y} onto the discrete output space that has not been part of the training data manifold. This means that according to Eq. (4) a neuron $c(\mathbf{y})$ with reference vector $\mathbf{m}_{c(\mathbf{y})}$ is activated for which

$$\|\mathbf{y} - \mathbf{m}_{c(\mathbf{y})}\| = \min_i \{\|\mathbf{y} - \mathbf{m}_i\|\} \quad (7)$$

The “image” $c(\mathbf{y})$ of the projected data item \mathbf{y} then represents the domain of input data patterns from X that is most similar to \mathbf{y} . Moreover, as the number of neurons N is much smaller than the number of vectors used for the training, this neuron will be sensitized and associated to a number of input data patterns from X which will represent the domain of input data patterns that is closest to \mathbf{y} .

2.2 The experimental setup

In our example 4000 residual time series (i.e. the element-wise difference between the simulated and the observed time series vectors) constituted the input data vectors of the training data set. The model time series were obtained from 4000 Monte Carlo simulations with the distributed conceptual watershed model NASIM running at hourly time steps over a period of two years, i.e. each input data vector consisted of 17 472 elements. Before the training, normalization of the data after Eq. (8) was carried out to avoid that high data values (vector elements) dominate the training because of their higher impact on the Euclidean distance measure Eq. (3) (Vesanto et al., 2000). Each

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element of the input data vectors is normalized to a variance of one and zero mean value using the linear transformation

$$x' = (x - \bar{x}) / \sigma_x \tag{8}$$

A coarse training period of 500 iterations with a large radius for the neighbourhood function was performed followed by a fine tuning period comprising 100 000 training cycles with short neighbourhood radius. In order to compare the results of the aforementioned Monte-Carlo simulation and the properties of the SOM, seven measures of performance, listed in Table 2, were calculated for each model run. Consecutively, a reference data set, which has not been part of the training data, consisting of the time series of observed data was projected onto the SOM according to Sect. 2.1. The resulting time series from this experiment will finally be evaluated visually as well as by means of different diagnostic plots. To ascertain whether the type of data used for the training exerts any influence on the SOM result the experiments were repeated with a SOM trained on discharge time series instead of residual time series.

2.3 The NASIM model and the data

NASIM is a distributed conceptual rainfall-runoff model (Hydrotec, 2005). It uses non-linear storage elements to simulate the soil water balance on spatially homogeneous units with respect to soil and land use, which themselves are subdivided into soil layers. NASIM is being commercially distributed since the mid-eighties and since then has found widespread application, e.g. in communal water resources management, throughout Germany. The details of the model are beyond the scope of this contribution. Instead, we adopt the decision-maker's point of view and treat the model as a black-box. Seven parameters were selected for Monte-Carlo random sampling (Table 1). The parameters were chosen to be identical to those that participated in the course of a manual expert calibration for the test watershed. Their bounds reflect the feasible parameter space based on the experience of this calibration. The input data for the model was taken from the 129 km² low-mountain range test watershed "Schwarze

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Pockau” Saxony (Germany), situated near the border to Czechoslovakia and tributary of the Freiburger Mulde, a sub-basin of the Elbe River. The period from 1 November 1994 to 28 October 1996 with hourly discharge and precipitation measurements was chosen to drive the Monte-Carlo simulation.

3 Results

In the first part of this section the properties of the SOM trained on residual time series and the relation of its elements to the traditional performance measures are examined. The second part is dedicated to testing the projection of measured data onto the SOM.

3.1 Testing the properties of the SOM

After the training each neuron of the 22×15 SOM is expected to be activated by a narrow domain of residual patterns from the input data manifold. The neurons and their respective location on the map are identifiable by index numbers. As the number of neurons is still much smaller than the number of model realizations used for the training, each neuron represents a set of Monte-Carlo model realizations that are characterized through similar temporal patterns with respect to their residuals or discharge values respectively. Because of the topographic ordering principle neighbouring map units, in turn, are expected to be “tuned” to similar residual patterns as well. Because the model realizations used for the training can be referenced by their corresponding index number on the map, the ordering principles of the “semantic map” represented by the SOM can be examined. To this end, the means of different performance measures as well as the mean values of the model parameters on each map element are calculated. This allows to assess the properties of the map’s ordering principle with respect to well known attributes such as a) the distribution of performance measures and b) the distribution of different model parameter values over the map lattice. Referring to a) seven performance measures have been calculated for each model realization

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(Table 2). For each of them individual SOM lattices were colour-coded according to the mean of the performance measure of the model runs associated with each map unit. Figure 1 shows the distribution of the performance measures from Table 2 on the SOM lattice. The same procedure was repeated for the Monte-Carlo parameters such that the distribution of mean parameter values can be shown for each parameter individually (Fig. 2). In each lattice of Fig. 1 and Fig. 2 the positions of the neurons remain identical such that each map element refers to identical model realizations in both figures.

As a striking feature of Fig. 1 it can be seen that, without providing explicit information about the performance measures with the training data, the different performance values are not distributed randomly across the map but significantly relate to different regions of the lattices. To interpret Fig. 1 it is important to notice that warm colours always correspond to high mean values and vice-versa, irrespective of whether this quality is associated with high or low goodness of fit. As to Fig. 2, a visibly ordered relation of the map regions to different parameter values can only be stated for two parameters (RetInf and maxInf), whereas the values of RetOf, StFFRet and vL do not appear to relate to any ordering principle. A similar random pattern can be observed for the two remaining parameters throughout wide areas of the map. However some intercalated areas in these lattices notably display again a relationship towards the parameter values, as can be seen from the locally ordered colour distribution. To facilitate the interpretation of these findings we compared Fig. 2 with scatterplots of performance measures. Figure 3 indicates that only the parameters RetInf and maxInf are sensitive with reference to the RMSE. Scatterplots for the remaining objective functions in Table 2 yielded the same results. Results identical to Fig. 1 and Fig. 2 were obtained by training a SOM on discharge time series instead of residual values.

3.2 Projecting the observed time series onto the SOM

To locate the best-matching unit (BMU) of the measured discharge (i.e. zero-residual) time series on the map, according to Sect. 2.1, an input vector consisting of elements

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with value 0 is constructed. Subsequently, in order to be projected properly along with the training data, the transformation Eq. (7) is carried out using the normalization parameters obtained from the input data set. In Fig. 4 the location of the resulting vector is displayed on top of the performance measure distributions shown in Fig. 1. It can be seen that the position of this BMU clearly does not coincide with any of the expected objective function optima or with the region where the combined optimum of the seven performance measures has to be expected approximately (outlined by the black rectangle in Fig. 4). Additionally, Table 3 summarizes the parameter values of the 11 model realizations that are associated to the BMU for representing the model time series that are most “similar” to a “perfect match” (i.e. the zero-residual case). By comparing these parameters of the corresponding model runs to the ranges in Table 1 it becomes obvious that, with the exception of RetInf and maxInf, all parameter values span the full range of the Monte-Carlo sampling bounds. All model realizations attached to this BMU have in common that only the mentioned parameter values appear to be narrowly constrained between 4.336 and 4.787 for RetInf and 0.107 and 0.134 for maxInf respectively. The resulting model outputs for these 11 realizations is shown in Fig. 5c along with the total envelope range of all 4000 simulation outputs in the background and the observed discharge. In order to better point out the differences between the hydrographs only the characteristic time period from 14 January 1995 to 21 October 1995 is reproduced. It can be seen that, compared to the whole set of Monte-Carlo outputs, these realizations obviously comprise a compact subset of “similar” time series. Additionally, the model results obtained from an expert manual calibration and the single-objective automatic calibration using the SCE-UA algorithm (Duan et al., 1993) with the RMSE as objective function (Table 2) are shown in Fig. 5. Although the SOM procedure, unlike the manual calibration, emphasizes all features of the hydrograph equally, the time series associated to the BMU of the measured discharge appear to outperform the result of the expert calibration (Fig. 5a). Compared to the SCE-UA result (Fig. 5b) the model realizations obtained from the SOM display a more accurate dynamic in the peaks and a better reproduction of the recession limbs.

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In Table 4 this visual impression can partly be corroborated by comparing the model results referring again to the formerly calculated performance measures from Table 2. The training on discharge data time series yielded identical results with respect to the position of the BMU on the SOM as well as the model realizations that were associated to it. It is interesting to note that, for both species of input data, the distributions of performance measures and parameter values throughout the map already ended up close to identical to those in Fig. 1 and Fig. 2 after only 1000 training cycles, whereas the identification of the BMU with the model realizations that are most similar to the observed values requires a number of training cycles that is at least one order of magnitude higher.

4 Discussion and conclusions

The performance measures that are linked to the map in Fig. 1 already indicate that very individual properties of the training data time series can be attributed to each element of the Self-Organizing Map. Furthermore, from the patterns of the performance measures on Fig. 1 it can be seen that certain correlation structures inherent to these statistical measures appear to be reflected by the map. Henceforth, we deduce that the information that can be extracted by these aggregating statistical measures is assimilated and preserved by the SOM. The findings with respect to Fig. 2, corroborated by Fig. 3 and Table 3, demonstrate that the SOM application is capable of revealing information about parameter sensitivities. Hence, we infer that the zones of only locally ordered parameter mean values in Fig. 2 (RetBasis and hL) indicate that the corresponding parameters are subject to interaction with other parameters. We consider this a further indication of the high discriminatory power of the SOM application with respect to the characteristics of different simulated discharge time series. This is because we were not able to obtain similar findings with traditional methods that are based on the evaluation of performance measures, e.g. parameter response surfaces for different objective functions.

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These useful aspects of the method are complemented by the findings of the second experiment: It demonstrates that the information which is processed by the SOM allows differentiating the spectrum of model realizations, given with the Monte-Carlo data, such that a rather narrowly confined set of model time series which are similar to the observed time series can be identified. It is important to notice that the results were achieved without resorting to aggregating statistical measures and therefore, the “similarity” represented in the SOM is not directly quantifiable in traditional terms. Instead, it rather accounts for the complexity that is inherent to time series data and which cannot be reduced to a rank number. Although the method is deterministic and the results are entirely reproducible, the resulting time series (Fig. 5c) can be further judged only subjectively. The fact that the experiments yielded identical results when the training was carried out using discharge data underpins the stability of the SOM method. Its resolution, of course, is dependent upon the number of model time series that participated in the training. The results (Fig. 5) which were achieved with a rather small number of model data items indicate that the SOM has the potential to be considered as an alternative to classical optimization algorithms. At this stage this issue still has to be subjected to more in-depth examination. The discriminatory power of the SOM that has been demonstrated in this article also highlights that uncertainty induced by the properties of the performance measure should be included in the discussion of model uncertainties and equifinality, because any statement on model behaviour depends on our possibilities to differentiate between model time series.

Acknowledgements. The authors wish to thank O. Buchholz (Hydrotec GmbH) and R. Wengel for their support. This work was carried out using the SOM-Toolbox for Matlab by the “SOM Toolbox Team” at the Helsinki University of Technology (<http://www.cis.hut.fi/projects/somtoolbox>)

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Table 1. Free NASIM model parameters of the Monte-Carlo simulation with their respective parameter ranges.

Name	Description	Range
RetBasis	Storage coefficient for baseflow component [h]	0.5–3.5
RetInf	Storage coefficient for interflow component [h]	2.0–6.0
RetOf	Storage coefficient for surface runoff from unsealed surfaces [h]	2.0–6.0
StFFRet	Storage coefficient for surface runoff from urban areas [h]	2.0–6.0
hL	Horizontal hydraulic conductivity factor	2.0–8.0
maxInf	Maximum infiltration factor	0.025–1.025
vL	Vertical hydraulic conductivity factor	0.005–0.105

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Table 2. Statistical goodness-of-fit measures calculated for the model output (Qobs: observed discharge, Qsim: simulated discharge).

Name	Description	Formula
BIAS	Mean error	$\frac{1}{N} \sum_{k=1}^N (Q_{\text{obs}} - Q_{\text{sim}_k})$
RMSE	Root of mean squared error	$\sqrt{\frac{1}{N} \sum_{k=1}^N (Q_{\text{obs}} - Q_{\text{sim}_k})^2}$
CEFFlog	Logarithmized Nash-Sutcliffe coefficient of efficiency	$\frac{\sum_{k=1}^N (\ln(Q_{\text{obs}}) - \ln(Q_{\text{sim}_k}))^2}{\sum_{k=1}^N (\ln(Q_{\text{obs}}) - \ln(\bar{Q}_{\text{obs}}))^2}$
IAG	Willmott's index of agreement (Willmott, 1981, 1982) $0 \leq \text{IAG} \leq 1$	$1 - \frac{\sum_{k=1}^N (Q_{\text{obs}} - Q_{\text{sim}_k})^2}{\sum_{k=1}^N (Q_{\text{sim}_k} - \bar{Q}_{\text{obs}} + Q_{\text{obs}} - \bar{Q}_{\text{obs}})^2}$
MAPE	Mean average percentual error	$\frac{100}{N} \sum_{k=1}^N \frac{1}{Q_{\text{obs}}} Q_{\text{sim}_k} - Q_{\text{obs}} $
VarMSE	Variance part of the mean squared error	$\sqrt{\frac{1}{N} \sum_{k=1}^N (Q_{\text{obs}} - \bar{Q}_{\text{obs}})^2} - \sqrt{\frac{1}{N} \sum_{k=1}^N (Q_{\text{sim}} - \bar{Q}_{\text{sim}})^2}$
Rlin	Coefficient of determination	$\frac{\sum_{k=1}^N [(Q_{\text{sim}} - \bar{Q}_{\text{sim}})(Q_{\text{obs}} - \bar{Q}_{\text{obs}})]}{\sqrt{\sum_{k=1}^N (Q_{\text{sim}} - \bar{Q}_{\text{sim}})^2 \sum_{k=1}^N (Q_{\text{obs}} - \bar{Q}_{\text{obs}})^2}}$

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Table 3. Summary of the parameter values of the 11 model realizations associated to the Best-Matching map Unit when the time series vector of observed discharges is projected onto the SOM.

	RetBasis	RetInf	RetOf	StFFRet	hL	maxInf	vL
min	0.699	4.336	2.379	2.202	2.191	0.107	0.008
max	3.143	4.787	5.731	5.581	6.540	0.134	0.105
mean	1.756	4.555	4.278	3.548	4.674	0.122	0.065

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Table 4. Comparison of model performances for results obtained from manual calibration, optimization with SCE-UA and the SOM application. In case of the SOM mean values of 11 results are given.

	BIAS	RMSE	CEFFlog	I _{Ag}	MAPE	VARmse	R _{lin}
manual calibration	0.32	1.58	0.50	0.86	42.36	0.01	0.75
SCE-UA optimization	0.08	1.69	0.47	0.84	38.26	0.00	0.72
SOM (means)	0.13	1.34	0.30	0.88	40.71	0.19	0.81

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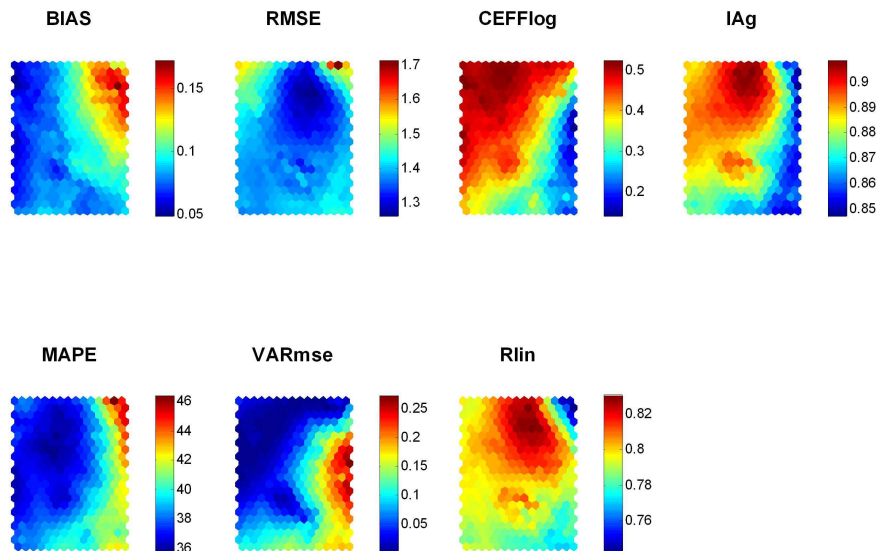


Fig. 1. Distribution of the mean values of each performance measure from Table 2 over the SOM lattice.

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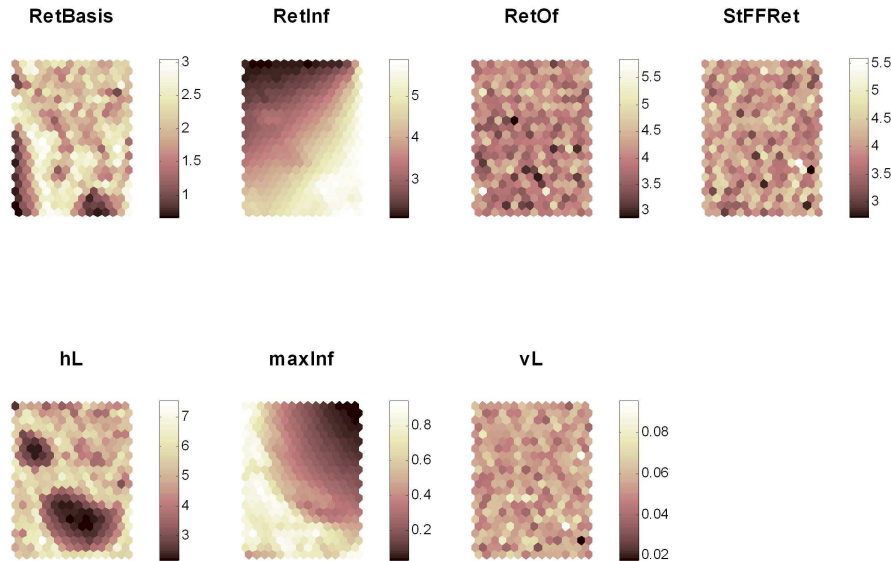


Fig. 2. Distribution of the mean values of each model parameter from Table 1 over the SOM lattice.

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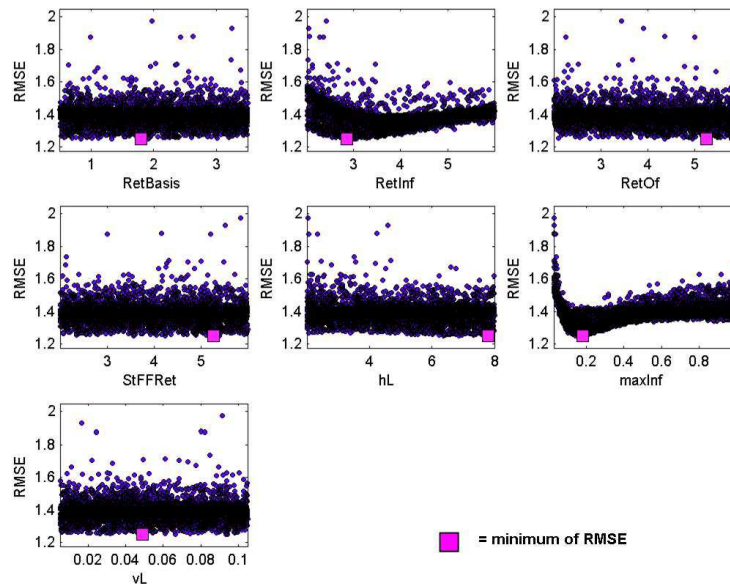


Fig. 3. Scatterplots of RMSE values for each of the examined NASIM parameters.

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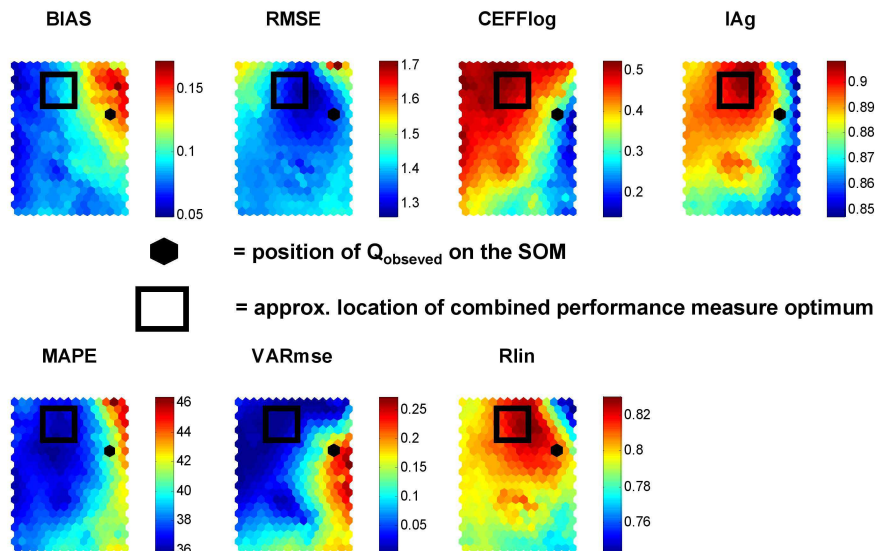


Fig. 4. The location of the best-matching unit (indicated by the black dot) for an input vector that represents the measured discharge time series. The rectangle outlines the region on the map where approximately a combined optimum of the seven performance measures has to be expected.

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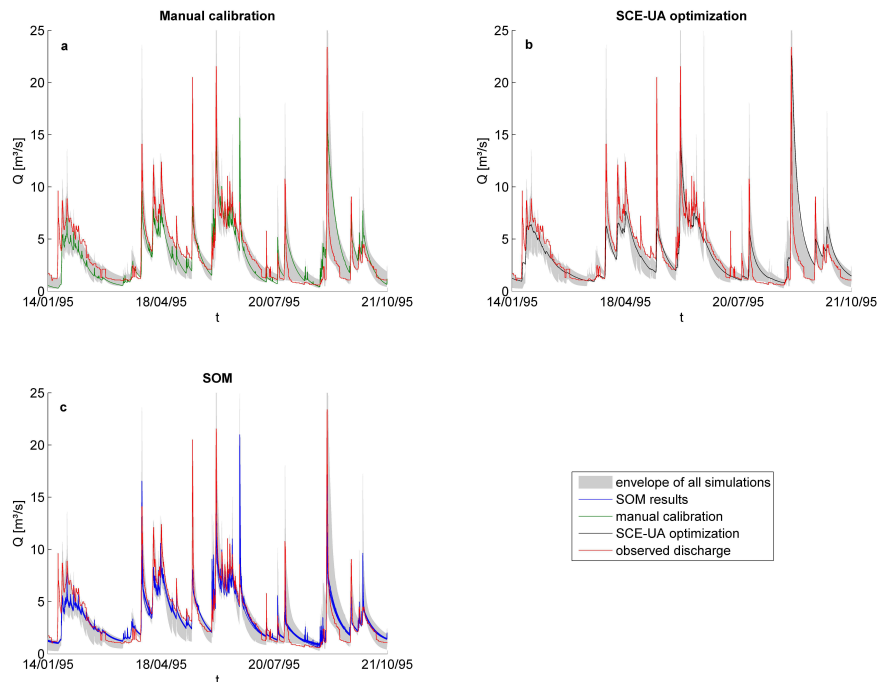


Fig. 5. The model realizations as resulting from (a) manual calibration, (b) optimization with the SCE-UA algorithm and (c) the BMU of the SOM for the measured discharge time series. The time-series are compared to the measured discharge and the envelope of the Monte-Carlo simulation, i.e. the area which is spanned by all model time series for the bounds given in Table 1.

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